

Vapor–Liquid Equilibrium in Binary Systems Ethanol + C4 and C5 Hydrocarbons

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Isothermal vapor–liquid equilibrium data are measured for seven binary systems containing ethanol and different C4 and C5 hydrocarbons: *cis*-but-2-ene, *trans*-but-2-ene, 2-methyl-but-2-ene, pent-1-ene, 2-methyl-but-1-ene, cyclopentene, and cyclopentane. The experimental synthetic method does not require the sampling of the vapor and liquid phases. The results were correlated by Peng–Robinson equation of state with the Huron–Vidal mixing rules.

Introduction

Alcohols and ethers are being considered as octane enhancers without lead. Among the last ones methyl *tert*-butyl ether (MTBE), ethyl *tert*-butyl ether (ETBE), and *tert*-amyl methyl ether (TAME) are undoubtedly the most studied compounds. A typical plant for the production of ETBE can be ideally divided into two sections:

(1) a reaction section, in which all the chemical reactions necessary for the production of ETBE, as well as secondary reactions, take place;

(2) a separation section, in which the blending agent is separated from the other compounds and in which these compounds are also separated for their recycle.

The optimization of the separation section and the simulation of the whole process require the use of thermodynamic models that should predict with precision the vapor–liquid equilibria and in particular the presence of azeotropes for the compounds presents in the separation section. These include a C₄–C₅ hydrocarbon blend from the feed, ethanol and other alcohols from the feed, and secondary reactions and water from the secondary reactions as well as from a washing tower used for cleaning the hydrocarbon blend.

For this reason new experimental data for ethanol with various C4 and C5 hydrocarbons are presented.

Experimental Section

Apparatus and Procedure. The experimental equipment and the procedure have been described in details by Fransson et al. (1992). Measurements were made by the static method using well-degassed materials. From a knowledge of the volume of the cell, the masses of each component, the temperature, and the pressure and using an equation of state coupled with a flash algorithm the compositions of the liquid and vapor phases were calculated. The total volume of the cell was determined to be

(60.44 ± 0.05) cm³; the masses of the components were determined by successive weighing during the filling procedure with a precision balance (0.1 mg). The temperature stability of the thermostatic bath was 0.01 K. The temperature was measured with a platinum resistance thermometer (Thermo-Est, 100 Ω) calibrated using a reference thermometer (IPTS-68); the standard deviation in temperature was 0.005 K. The pressure was measured with a pressure transducer, and the expected standard deviation was 1.8 kPa.

Chemicals. The chemicals that are used are *cis*-but-2-ene, *trans*-but-2-ene with a purity higher than 99.5% from Praxair, 2-methyl-but-2-ene, pent-1-ene, 2-methyl-but-1-ene, cyclopentene, and cyclopentane with a purity higher than 99% from Fluka AG and ethanol with a purity higher than 99.9% from C. Erba. The ethanol was stored over molecular sieves 5 Å in order to reduce the water content.

To check the purity of the products and the reliability of our equipment, vapor pressure data were measured (Table 1) for the C4 and C5 hydrocarbons and compared with values reported in the literature (DIPPR, 1989). It is important to note that the accuracy of the correlation reported in the literature (DIPPR, 1989) is not better than 3%. For that reason since the relative deviations are always lower it is possible to be satisfied both for the performance of the equipment and for the purity of the chemicals used. Some duplicated or triplicated measurements were also performed in order to check the repeatability of the measurements. Also this check was very satisfactory.

Results and Discussion

The quantities experimentally determined are the temperature *T*, the pressure *P*, the total volume, and the masses of each compound *m*₁ and *m*₂, which give the overall mole fraction *z*_{*i*}. These data are reported for the different systems studied in the Tables 2–8. The liquid *x*_{*i*} and the

Table 1. Vapor Pressures P of Pure Hydrocarbons at Temperature T : Literature (lit) Values Obtained by Interpolation from DIPPR (1989) and Percent Relative Deviation

| product | T/K | P/bar | $P_{\text{lit}}/\text{bar}$ | $100 P - P_{\text{lit}}/P $ |
|-------------------------|--------|----------------|-----------------------------|-----------------------------|
| <i>cis</i> -but-2-ene | 323.68 | 4.577 | 4.499 | 1.74 |
| | 323.75 | 4.549 | 4.507 | 0.93 |
| | 374.46 | 1.498 | 14.436 | 0.42 |
| <i>trans</i> -but-2-ene | 374.56 | 14.503 | 14.465 | 0.26 |
| | 323.76 | 4.897 | 4.902 | -0.10 |
| | 323.79 | 4.875 | 4.906 | -0.64 |
| | 374.56 | 15.378 | 15.691 | -2.0 |
| 2-methyl-but-2-ene | 374.59 | 15.372 | 15.701 | -2.09 |
| | 323.66 | 6.177 | 6.235 | -0.93 |
| | 323.79 | 6.144 | 6.256 | -1.79 |
| | 323.75 | 6.194 | 6.249 | -0.88 |
| | 323.83 | 6.194 | 6.262 | -1.08 |
| | 374.45 | 18.563 | 18.879 | -1.67 |
| | 374.52 | 18.569 | 18.904 | -1.77 |
| | 374.53 | 18.693 | 18.907 | -1.13 |
| pent-1-ene | 374.59 | 18.642 | 18.929 | -1.52 |
| | 323.44 | 1.948 | 1.951 | -0.15 |
| | 323.33 | 1.946 | 1.944 | 0.10 |
| | 373.54 | 7.002 | 6.954 | 0.69 |
| | 373.53 | 7.004 | 6.953 | 0.73 |
| 2-methyl-but-1-ene | 323.42 | 1.886 | 1.886 | 0 |
| | 323.40 | 1.891 | 1.885 | 0.32 |
| | 323.43 | 1.890 | 1.887 | 0.16 |
| | 323.42 | 1.891 | 1.886 | 0.27 |
| | 373.56 | 6.879 | 6.875 | 0.058 |
| | 373.51 | 6.878 | 6.867 | 0.16 |
| | 373.54 | 6.875 | 6.872 | 0.27 |
| | 323.50 | 1.061 | 1.050 | 1.05 |
| cyclopentane | 323.44 | 1.067 | 1.048 | 1.81 |
| | 323.40 | 1.059 | 1.047 | 1.15 |
| | 323.41 | 1.061 | 1.047 | 1.34 |
| | 373.58 | 4.208 | 4.204 | 0.095 |
| | 373.61 | 4.200 | 4.207 | -0.17 |
| | 373.59 | 4.201 | 4.205 | -0.095 |
| | 323.37 | 1.244 | 1.233 | 0.89 |
| cyclopentene | 323.38 | 1.248 | 1.233 | 1.21 |
| | 323.42 | 1.249 | 1.235 | 1.13 |
| | 323.43 | 1.247 | 1.235 | 0.97 |
| | 373.49 | 4.850 | 4.830 | 0.41 |
| | 373.62 | 4.850 | 4.845 | 0.10 |
| | 373.53 | 4.853 | 4.835 | 0.37 |

vapor y_i mole fractions were obtained according to the procedure suggested by Fransson et al. (1992), applying an equation of state to the whole set of experimental data.

Thermodynamic Models. We have used the Peng–Robinson model (Peng and Robinson, 1976) associated with the volume correction proposed by Peneloux (Peneloux and Rauzy, 1982).

$$P = \frac{RT}{v-b} - \frac{a(T)}{v(v+b) + b(v-b)} \quad (1)$$

$$a = a_c [1 + m(1 - T_r^{0.5})]^2 \quad T_r = T/T_c \quad (2)$$

The m parameter was fitted to force the equation of state to calculate the experimental vapor pressure of the pure components.

The volume correction c was considered independent of the temperature. It was calculated from the saturated molar volume at 293 K given in the DIPPR Data Compilation (DIPPR, 1989).

$$V_{\text{corr},i} = V_i - C_i \quad (3)$$

$$c = \sum_i C_i Z_i \quad (4)$$

The parameter b of the equation was calculated with the

Table 2. Experimental and Calculated Data for the *cis*-But-2-ene (1) + Ethanol (2) System: Masses m_i , Overall Mole Fractions z_i , Temperature T , Pressure P , Liquid Mole Fractions x_i , Vapor Mole Fractions y_i

| m_1/g | m_2/g | z_1 | T/K | P/bar | $P_{\text{calc}}/\text{bar}$ | x_1 | y_1 |
|----------------|----------------|-------|--------|----------------|------------------------------|--------|--------|
| 20.1165 | 0.2524 | 0.985 | 323.72 | 4.51 | 4.55 | 0.9849 | 0.9868 |
| 22.3172 | 0.82 | 0.957 | 323.75 | 4.54 | 4.53 | 0.9570 | 0.9715 |
| 22.6133 | 1.9964 | 0.903 | 323.81 | 4.52 | 4.48 | 0.9024 | 0.9579 |
| 17.8409 | 6.248 | 0.701 | 323.74 | 4.34 | 4.35 | 0.6986 | 0.9484 |
| 14.7277 | 11.6357 | 0.510 | 323.81 | 4.17 | 4.17 | 0.5063 | 0.9424 |
| 9.6121 | 17.4238 | 0.312 | 323.75 | 3.59 | 3.59 | 0.3078 | 0.9274 |
| 2.9279 | 24.6622 | 0.089 | 50.59 | 1.82 | 1.82 | 0.0865 | 0.8404 |
| 20.1165 | 0.2524 | 0.985 | 374.55 | 14.62 | 14.57 | 0.9850 | 0.9825 |
| 22.3172 | 0.82 | 0.957 | 374.53 | 14.62 | 14.61 | 0.9572 | 0.9567 |
| 22.6133 | 1.9964 | 0.903 | 374.55 | 14.58 | 14.53 | 0.9025 | 0.9230 |
| 17.8409 | 6.248 | 0.701 | 374.57 | 13.71 | 13.77 | 0.6970 | 0.8711 |
| 14.7277 | 11.6357 | 0.510 | 374.54 | 12.87 | 12.85 | 0.5035 | 0.8460 |
| 9.6121 | 17.4238 | 0.312 | 374.57 | 10.96 | 10.97 | 0.3039 | 0.8036 |
| 2.9279 | 24.6622 | 0.089 | 374.52 | 5.91 | 5.91 | 0.0847 | 0.6070 |

Table 3. Experimental and Calculated Data for the *trans*-But-2-ene (1) + Ethanol (2) System: Masses m_i , Overall Mole Fractions z_i , Temperature T , Pressure P , Liquid Mole Fractions x_i , Vapor Mole Fractions y_i

| m_1/g | m_2/g | z_1 | T/K | P/bar | $P_{\text{calc}}/\text{bar}$ | x_{1c} | y_1 |
|----------------|----------------|-------|--------|----------------|------------------------------|----------|--------|
| 19.8336 | 0.3283 | 0.980 | 323.79 | 4.88 | 4.89 | 0.9802 | 0.9826 |
| 20.1261 | 1.1572 | 0.935 | 323.75 | 4.86 | 4.84 | 0.9342 | 0.9643 |
| 20.298 | 1.3649 | 0.924 | 323.79 | 4.85 | 4.83 | 0.9231 | 0.9621 |
| 17.0389 | 3.0689 | 0.820 | 323.70 | 4.78 | 4.75 | 0.8180 | 0.9543 |
| 19.3797 | 6.2833 | 0.717 | 323.78 | 4.68 | 4.70 | 0.715 | 0.9518 |
| 15.2772 | 11.6108 | 0.519 | 323.73 | 4.41 | 4.46 | 0.5161 | 0.9453 |
| 8.8683 | 9.5030 | 0.434 | 323.86 | 4.30 | 4.27 | 0.4251 | 0.9401 |
| 3.8539 | 25.5387 | 0.110 | 323.76 | 2.36 | 2.36 | 0.1077 | 0.8765 |
| 19.8336 | 0.3283 | 0.980 | 374.52 | 15.46 | 15.46 | 0.9804 | 0.9772 |
| 20.1261 | 1.1572 | 0.935 | 374.52 | 15.50 | 15.49 | 0.9344 | 0.9404 |
| 20.298 | 1.3649 | 0.924 | 374.51 | 15.47 | 15.47 | 0.9233 | 0.9340 |
| 17.0389 | 3.0689 | 0.820 | 374.50 | 15.15 | 15.09 | 0.8169 | 0.8955 |
| 19.3797 | 6.2833 | 0.717 | 374.60 | 14.66 | 14.69 | 0.7141 | 0.8764 |
| 15.2772 | 11.6108 | 0.519 | 374.57 | 13.63 | 13.67 | 0.5137 | 0.8506 |
| 8.8683 | 9.5030 | 0.434 | 374.62 | 12.96 | 12.93 | 0.4140 | 0.8351 |
| 3.8539 | 25.5387 | 0.110 | 374.53 | 7.213 | 7.21 | 0.1057 | 0.6752 |

classical mixing rule:

$$b = \sum_i \sum_j x_i x_j b_{ij} \quad (5)$$

$$b_{ij} = \frac{b_i + b_j}{2} \quad (6)$$

For the evaluation of a parameter, the Huron–Vidal approach (Huron and Vidal, 1979) was followed

$$a = b \cdot \left[\sum_{i=1}^N x_i \frac{a_{ii}}{b_i} - \frac{g_{\infty}^E}{\Lambda} \right] \quad (7)$$

where Λ is a numerical constant depending on the cubic equation of state used: for the Peng–Robinson equation its value is given by the following expression:

$$\Lambda = \frac{1}{2 \cdot \sqrt{2}} \ln \left[\frac{2 + \sqrt{2}}{2 - \sqrt{2}} \right] \quad (8)$$

g_{∞}^E , excess Gibbs energy at infinite pressure, is expressed with the N.R.T.L. model (Renon and Prausnitz, 1978) in which the concentrations are expressed in terms

Table 4. Experimental and Calculated Data for the 2-Methyl-but-2-ene (1) + Ethanol (2) System: Masses m_i , Overall Mole Fractions z_i , Temperature T , Pressure P , Liquid Mole Fractions x_i , Vapor Mole Fractions y_i

| m_1/g | m_2/g | z_1 | T/K | P/bar | $P_{\text{calc}}/\text{bar}$ | x_1 | y_1 |
|---------|---------|-------|--------|----------------|------------------------------|--------|--------|
| 18.0087 | 0.3326 | 0.978 | 323.80 | 6.14 | 6.16 | 0.9778 | 0.9842 |
| 15.2896 | 1.0552 | 0.922 | 323.80 | 6.13 | 6.07 | 0.9210 | 0.9695 |
| 18.8947 | 2.3757 | 0.867 | 323.78 | 5.97 | 6.00 | 0.8655 | 0.9655 |
| 16.4181 | 6.1735 | 0.686 | 323.79 | 5.79 | 5.82 | 0.6817 | 0.9603 |
| 13.5893 | 9.7131 | 0.535 | 323.78 | 5.52 | 5.49 | 0.5288 | 0.9545 |
| 7.2612 | 20.1951 | 0.228 | 323.81 | 4.06 | 4.07 | 0.2230 | 0.9296 |
| 3.2566 | 25.1649 | 0.096 | 323.78 | 2.68 | 2.68 | 0.0927 | 0.8886 |
| 18.0087 | 0.3326 | 0.978 | 374.59 | 18.65 | 18.69 | 0.9780 | 0.9775 |
| 15.2896 | 1.0552 | 0.922 | 374.50 | 18.47 | 18.50 | 0.9207 | 0.9415 |
| 18.8947 | 2.3757 | 0.867 | 374.53 | 18.11 | 18.21 | 0.8650 | 0.9218 |
| 16.4181 | 6.1735 | 0.686 | 374.61 | 17.05 | 17.04 | 0.6785 | 0.8878 |
| 13.5893 | 9.7131 | 0.535 | 374.56 | 15.86 | 15.77 | 0.5233 | 0.8663 |
| 7.2612 | 20.1951 | 0.228 | 374.53 | 11.28 | 11.32 | 0.2189 | 0.7919 |
| 3.2566 | 25.1649 | 0.096 | 374.64 | 7.49 | 7.48 | 0.0905 | 0.6785 |

Table 5. Experimental and Calculated Data for the Pent-1-ene (1) + Ethanol (2) System: Masses m_i , Overall Mole Fractions z_i , Temperature T , Pressure P , Liquid Mole Fractions x_i , Vapor Mole Fractions y_i

| m_1/g | m_2/g | z_1 | T/K | P/bar | $P_{\text{calc}}/\text{bar}$ | x_1 | y_1 |
|---------|---------|-------|--------|----------------|------------------------------|--------|--------|
| 4.1141 | 22.2639 | 0.108 | 323.39 | 1.14 | 1.15 | 0.1068 | 0.7571 |
| 9.4065 | 17.0065 | 0.267 | 323.49 | 1.67 | 1.65 | 0.2646 | 0.8436 |
| 14.9441 | 13.2154 | 0.426 | 323.43 | 1.85 | 1.87 | 0.4248 | 0.8722 |
| 20.0218 | 7.7981 | 0.628 | 323.39 | 1.98 | 1.98 | 0.6269 | 0.8873 |
| 22.2045 | 5.0401 | 0.743 | 323.42 | 1.99 | 2.00 | 0.7427 | 0.8914 |
| 23.5520 | 2.7377 | 0.850 | 323.39 | 2.02 | 2.01 | 0.8495 | 0.8985 |
| 25.3915 | 1.5748 | 0.914 | 323.41 | 2.03 | 2.02 | 0.9137 | 0.9133 |
| 26.8203 | 0.2532 | 0.986 | 323.39 | 2.01 | 1.98 | 0.9859 | 0.9735 |
| 4.1141 | 22.2639 | 0.108 | 373.52 | 4.66 | 4.66 | 0.1051 | 0.5340 |
| 9.4065 | 17.0065 | 0.267 | 373.61 | 6.33 | 6.31 | 0.2624 | 0.6787 |
| 14.9441 | 13.2154 | 0.426 | 373.60 | 7.03 | 7.06 | 0.4235 | 0.7337 |
| 20.0218 | 7.7981 | 0.628 | 373.54 | 7.46 | 7.47 | 0.6265 | 0.7743 |
| 22.2045 | 5.0401 | 0.743 | 373.56 | 7.59 | 7.60 | 0.7427 | 0.7986 |
| 23.5520 | 2.7377 | 0.850 | 373.56 | 7.63 | 7.64 | 0.8498 | 0.8355 |
| 25.3915 | 1.5748 | 0.914 | 373.59 | 7.56 | 7.55 | 0.9141 | 0.8768 |
| 26.8203 | 0.2532 | 0.986 | 373.57 | 7.27 | 7.15 | 0.9860 | 0.9701 |

Table 6. Experimental and Calculated Data for the 2-Methyl-but-1-ene (1) + Ethanol (2) System: Masses m_i , Overall Mole Fractions z_i , Temperature T , Pressure P , Liquid Mole Fractions x_i , Vapor Mole Fractions y_i

| m_1/g | m_2/g | z_1 | T/K | P/bar | $P_{\text{calc}}/\text{bar}$ | x_1 | y_1 |
|---------|---------|-------|--------|----------------|------------------------------|--------|--------|
| 6.7815 | 21.3460 | 0.173 | 323.41 | 1.334 | 1.338 | 0.1713 | 0.8000 |
| 11.9464 | 16.6728 | 0.32 | 323.44 | 1.693 | 1.676 | 0.3186 | 0.8520 |
| 18.5555 | 9.6451 | 0.558 | 323.41 | 1.879 | 1.897 | 0.5572 | 0.8827 |
| 22.0608 | 5.2175 | 0.735 | 323.41 | 1.933 | 1.942 | 0.7347 | 0.8915 |
| 24.5825 | 2.2020 | 0.880 | 323.42 | 1.965 | 1.960 | 0.8799 | 0.9033 |
| 25.9346 | 0.8604 | 0.952 | 323.42 | 1.967 | 1.955 | 0.9520 | 0.9334 |
| 27.2525 | 0.2977 | 0.978 | 323.47 | 1.967 | 1.935 | 0.9783 | 0.9610 |
| 6.7815 | 21.3460 | 0.173 | 373.59 | 5.284 | 5.292 | 0.1697 | 0.6045 |
| 11.9464 | 16.6728 | 0.32 | 373.55 | 6.451 | 6.422 | 0.3171 | 0.6987 |
| 18.5555 | 9.6451 | 0.558 | 373.58 | 7.193 | 7.223 | 0.5565 | 0.7638 |
| 22.0608 | 5.2175 | 0.735 | 373.55 | 7.440 | 7.455 | 0.7347 | 0.7997 |
| 24.5825 | 2.2020 | 0.880 | 373.58 | 7.478 | 7.479 | 0.8803 | 0.8527 |
| 25.9346 | 0.8604 | 0.952 | 373.58 | 7.289 | 7.274 | 0.9523 | 0.9157 |
| 27.2525 | 0.2977 | 0.978 | 373.52 | 7.125 | 7.089 | 0.9785 | 0.9552 |

of volumetric fractions at infinite pressure defined as

$$\phi_i = \frac{x_i^* b_i}{\sum_{i=1}^N x_i^* b_i} = \frac{x_i^* b_i}{b_m} \quad (9)$$

instead of mole fractions.

Table 7. Experimental and Calculated Data for the Cyclopentane (1) + Ethanol (2) System: Masses m_i , Overall Mole Fractions z_i , Temperature T , Pressure P , Liquid Mole Fractions x_i , Vapor Mole Fractions y_i

| m_1/g | m_2/g | z_1 | T/K | P/bar | $P_{\text{calc}}/\text{bar}$ | x_1 | y_1 |
|---------|---------|-------|--------|----------------|------------------------------|--------|--------|
| 7.2272 | 20.5213 | 0.188 | 323.44 | 0.959 | 0.962 | 0.1870 | 0.7214 |
| 12.0236 | 17.0298 | 0.317 | 323.38 | 1.099 | 1.088 | 0.3160 | 0.7681 |
| 17.0807 | 12.6155 | 0.471 | 323.45 | 1.166 | 1.172 | 0.4701 | 0.7978 |
| 23.2103 | 7.2102 | 0.679 | 323.36 | 1.204 | 1.206 | 0.6787 | 0.8173 |
| 23.9029 | 5.3019 | 0.748 | 323.44 | 1.205 | 1.211 | 0.7474 | 0.8189 |
| 27.6455 | 2.3039 | 0.887 | 323.46 | 1.207 | 1.210 | 0.8875 | 0.8249 |
| 29.2850 | 0.8626 | 0.957 | 323.42 | 1.183 | 1.173 | 0.9573 | 0.8680 |
| 7.2272 | 20.5213 | 0.188 | 373.55 | 4.417 | 4.422 | 0.1857 | 0.5314 |
| 12.0236 | 17.0298 | 0.317 | 373.56 | 4.934 | 4.896 | 0.3150 | 0.6021 |
| 17.0807 | 12.6155 | 0.471 | 373.63 | 5.193 | 5.204 | 0.4695 | 0.6541 |
| 23.2103 | 7.2102 | 0.679 | 373.53 | 5.303 | 5.333 | 0.6788 | 0.7034 |
| 23.9029 | 5.3019 | 0.748 | 373.55 | 5.313 | 5.335 | 0.7478 | 0.7178 |
| 27.6455 | 2.3039 | 0.887 | 373.56 | 5.198 | 5.200 | 0.8883 | 0.7670 |
| 29.2850 | 0.8626 | 0.957 | 373.63 | 4.867 | 4.841 | 0.9578 | 0.8502 |

Table 8. Experimental and Calculated Data for the Cyclopentene (1) + Ethanol (2) System: Masses m_i , Overall Mole Fractions z_i , Temperature T , Pressure P , Liquid Mole Fractions x_i , Vapor Mole Fractions y_i

| m_1/g | m_2/g | z_1 | T/K | P/bar | $P_{\text{calc}}/\text{bar}$ | x_1 | y_1 |
|---------|---------|-------|--------|----------------|------------------------------|--------|--------|
| 6.3734 | 21.6858 | 0.166 | 323.46 | 0.950 | 0.953 | 0.1649 | 0.7235 |
| 12.5024 | 16.3523 | 0.341 | 323.40 | 1.234 | 1.223 | 0.3399 | 0.8064 |
| 19.6672 | 11.2306 | 0.542 | 323.42 | 1.301 | 1.322 | 0.5416 | 0.8340 |
| 24.7867 | 7.1053 | 0.702 | 323.45 | 1.339 | 1.340 | 0.7020 | 0.8413 |
| 26.7273 | 4.9892 | 0.784 | 323.41 | 1.347 | 1.343 | 0.7836 | 0.8456 |
| 28.2575 | 2.8313 | 0.871 | 323.41 | 1.350 | 1.345 | 0.8710 | 0.8600 |
| 31.1045 | 1.2763 | 0.943 | 323.43 | 1.340 | 1.327 | 0.9429 | 0.9004 |
| 6.3734 | 21.6858 | 0.166 | 373.57 | 4.307 | 4.310 | 0.1637 | 0.5221 |
| 12.5024 | 16.3523 | 0.341 | 373.58 | 5.196 | 5.169 | 0.3387 | 0.6395 |
| 19.6672 | 11.2306 | 0.542 | 373.55 | 5.560 | 5.578 | 0.5412 | 0.7036 |
| 24.7867 | 7.1053 | 0.702 | 373.53 | 5.676 | 5.693 | 0.7021 | 0.7411 |
| 26.7273 | 4.9892 | 0.784 | 373.50 | 5.675 | 5.694 | 0.7838 | 0.7631 |
| 28.2575 | 2.8313 | 0.871 | 373.53 | 5.676 | 5.626 | 0.8715 | 0.8007 |
| 31.1045 | 1.2763 | 0.943 | 373.53 | 5.430 | 5.389 | 0.9432 | 0.8677 |

The final expression for a is

$$a = b \cdot \sum_{i=1}^N x_i^* \left[\frac{a_{ii}}{b_{ii}} - \frac{1}{\Lambda} \frac{\sum_{j=1}^N x_j^* G_{ji} \cdot C_{ji}}{\sum_{k=1}^N x_k^* G_{ki}} \right] \quad (10)$$

with

$$G_{ji} = b_j \exp\left(-\alpha_{ji} \frac{C_{ji}}{RT}\right) \quad (11)$$

where $\alpha_{ij} = \alpha_{ji}$, C_{ij} and C_{ji} with $C_{ii} = C_{jj} = 0$ and with are the parameters of the model.

For sake of comparison also the classical mixing rules with one binary parameter were also used:

$$a = \sum_i \sum_j x_i x_j a_{ij} \quad (12)$$

$$a_{ij} = (a_i a_j)^{0.5} (1 - k_{ij}) \quad (13)$$

The values of the critical properties and the acentric factor are given in Table 9 (DIPPR, 1989).

The calculation procedure starts with an initial guess of the binary interaction parameters for the model, and for each experimental point from the experimental measured

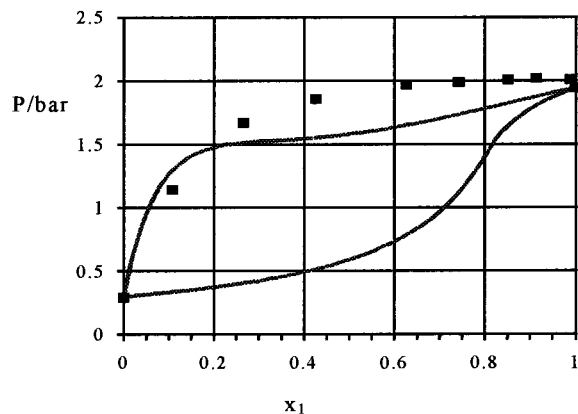


Figure 1. Correlation of the experimental data (■) for the system pent-1-ene (1) + ethanol (2) at 50.23 °C using the Peng–Robinson equation of state with classical mixing rules (—).

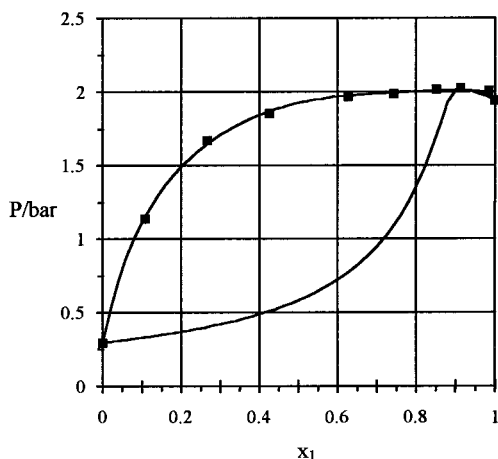


Figure 2. Correlation of the experimental data (■) for the system pentene-1 (1) + ethanol (2) at 50.23 °C using the Peng–Robinson equation of state with Huron Vidal mixing rules (—).

Table 9. Critical Temperature T_c , Critical Pressure P_c , and Acentric Factor ω for the Solutes Investigated

| compound | T_c /K | P_c /bar | ω |
|-------------------------|----------|------------|----------|
| <i>cis</i> -but-2-ene | 435.6 | 42.0 | 0.202 |
| <i>trans</i> -but-2-ene | 428.6 | 39.9 | 0.205 |
| 2-methyl-but-2-ene | 417.9 | 40.0 | 0.194 |
| pent-1-ene | 464.8 | 35.13 | 0.233 |
| 2-methyl-1-butene | 465.0 | 37.8 | 0.232 |
| cyclopentane | 511.7 | 45.1 | 0.196 |
| cyclopentene | 507.0 | 47.9 | 0.194 |
| ethanol | 513.9 | 61.4 | 0.644 |

Table 10. Comparison between Different Mixing Rules and EOS for the Exploitation of Experimental Data for the System 2-Methyl-but-2-ene + Ethanol: Results Are the Sums of the Squares of the Deviations in Pressures

| model | T/K | $\sum_i (P_i^{\text{calc}} - P)^2/\text{bar}^2$ |
|--------------|--------|---|
| PR classical | 323.38 | 0.372 |
| PRHV | 323.38 | 0.239×10^{-2} |
| RKSHV | 323.38 | 0.242×10^{-2} |
| PR classical | 373.53 | 2.33 |
| PRHV | 373.53 | 0.143×10^{-1} |
| RKSHV | 373.53 | 0.142×10^{-1} |

total volume, temperature, and masses of the two components the equilibrium pressure is calculated; in this step the vapor–liquid equilibrium is calculated using the equation-of-state model and the equilibrium conditions, and as a consequence the volumes of the vapor and liquid phases and their compositions are calculated. A mean quadratic

Table 11. Binary Interaction Parameters for the Systems Considered

| binary system | T/K | C_{ij}^1 ($\text{cm}^3 \text{ bar mol}^{-1}$) | C_{ij}^2 ($\text{cm}^3 \text{ bar mol}^{-1}$) | α |
|---|--------|--|--|----------|
| <i>cis</i> -but-2-ene (1) + ethanol (2) | 323.75 | 7468.69 | 2244.68 | 0.45 |
| | 374.54 | 6903.11 | 1782.17 | 0.44 |
| <i>trans</i> -but-2-ene (1) + ethanol (2) | 323.77 | 7883.91 | 2988.61 | 0.48 |
| | 374.55 | 7046.75 | 2552.28 | 0.48 |
| 2-methyl-but-2-ene (1) + ethanol (2) | 323.78 | 8053.19 | 3580.61 | 0.52 |
| | 374.56 | 7237.48 | 3324.91 | 0.56 |
| pent-1-ene (1) + ethanol (2) | 323.38 | 7734.16 | 2846.23 | 0.46 |
| | 373.53 | 7213.62 | 2582.93 | 0.46 |
| 2-methyl-but-1-ene (1) + ethanol (2) | 323.42 | 7670.87 | 2660.50 | 0.46 |
| | 373.54 | 7149.28 | 2282.25 | 0.46 |
| cyclopentane (1) + ethanol (2) | 323.44 | 8378.91 | 3822.05 | 0.44 |
| | 373.60 | 7996.22 | 4080.66 | 0.47 |
| cyclopentene (1) + ethanol (2) | 323.40 | 7061.46 | 1585.34 | 0.37 |
| | 373.55 | 6891.83 | 2687.50 | 0.46 |

Table 12. Mean Quadratic Relative Deviations in Pressure and Sums of the Squares of the Deviations in Pressures for the Different Binary Systems

| system | T/K | $100 \sigma_P\%$ | $\sum_i (P_i^{\text{calc}} - P_i^{\text{exp}})^2 \times 10^2$ |
|-----------------------------------|--------|------------------|---|
| <i>cis</i> -but-2-ene + ethanol | 323.75 | 0.47 | 0.31 |
| | 374.54 | 0.25 | 0.85 |
| <i>trans</i> -but-2-ene + ethanol | 323.77 | 0.56 | 0.52 |
| | 374.55 | 0.21 | 0.73 |
| 2-methyl-but-2-ene + ethanol | 323.78 | 1.44 | 4.78 |
| | 374.56 | 0.36 | 2.33 |
| pent-1-ene + ethanol | 323.38 | 0.90 | 0.24 |
| | 373.53 | 0.58 | 1.43 |
| 2-methyl-but-1-ene + ethanol | 323.42 | 0.87 | 0.19 |
| | 373.54 | 0.32 | 0.36 |
| cyclopentane + ethanol | 323.44 | 0.59 | 0.03 |
| | 373.60 | 0.45 | 0.36 |
| cyclopentene + ethanol | 323.40 | 0.82 | 0.08 |
| | 373.55 | 0.52 | 0.59 |

Table 13. Pressures and Azeotropic Compositions Calculated

| system | T/K | experimental azeotrope | calculated azeotrope | x_{az} | P_{az}/bar |
|-----------------------------------|--------|------------------------|----------------------|-----------------|----------------------------|
| <i>cis</i> -but-2-ene + ethanol | 323.75 | no | no | | |
| | 374.54 | no | yes | 0.954 | 14.61 |
| <i>trans</i> -but-2-ene + ethanol | 323.77 | no | yes | 0.990 | 4.89 |
| | 374.55 | yes | yes | 0.954 | 15.51 |
| 2-methyl-but-2-ene + ethanol | 323.78 | no | no | | |
| | 374.56 | no | yes | 0.978 | 18.68 |
| pent-1-ene + ethanol | 323.38 | no | yes | 0.914 | 2.02 |
| | 373.53 | yes | yes | 0.824 | 7.64 |
| 2-methyl-but-1-ene + ethanol | 323.42 | no | yes | 0.912 | 1.96 |
| | 373.54 | yes | yes | 0.812 | 7.50 |
| cyclopentane + ethanol | 323.44 | yes | yes | 0.820 | 1.21 |
| | 373.60 | yes | yes | 0.710 | 5.34 |
| cyclopentene + ethanol | 323.40 | yes | yes | 0.856 | 1.34 |
| | 373.55 | yes | yes | 0.754 | 5.70 |

relative deviation is calculated

$$\sigma_P = \sqrt{\frac{\sum_{i=1}^n \left(\frac{P_{\text{calc}} - P}{P} \right)^2}{n}} \quad (14)$$

where n is the number of experimental points. The optimum values of the parameters of the model are obtained minimizing σ_P .

The compositions of the phases calculated following this procedure depend on the model used and cannot be accepted if the correlation of the pressure is bad.

In Figures 1 and 2 the results obtained for the system pent-1-ene + ethanol using the Peng–Robinson equation of state but with the classical mixing rules (PR classical) and with the Huron–Vidal (PRHV) approach are reported. It is evident that the classical mixing rules are unable to reproduce the experimental pressures within the experimental accuracy. To check the influence of the equation-of-state model, the same calculations were repeated also with the Redlich–Kwong–Soave equation of state (Soave, 1972) and with the Huron–Vidal mixing rules (RKSHV). The deviations in terms of pressure are very close to those obtained with the Peng–Robinson EOS. In Table 10 the results obtained with the three different approaches for the system pent-1-ene + ethanol are reported. The influence of the mixing rules is evident, whereas the type of equation of state has no effect on the quality of the data reduction.

On the basis of these results, all the data were correlated using the Peng–Robinson equation of state with the Huron–Vidal mixing rules. The compositions of the liquid and vapor phases obtained are reported in Tables 2–8. In Table 11 the numerical values of the binary parameters for the different binary systems are given, and in Table 12 the deviations in pressures for the different systems are reported both in terms of sum of squares of the deviations and as σ_P (see eq 14). Deviations are reasonable: the only system showing larger deviations is the system containing 2-methyl-but-2-ene.

From the experimental pressures measured and from the numerical values of the parameters of the model, it is possible to calculate the composition and the corresponding pressures of the binary azeotropes for the systems considered: the results of these calculations are presented in Table 13 and compared with the experimental data. It is always possible to calculate the existence of experimentally

founded azeotropes; vice versa in some cases the model predicts the existence of azeotropes when there is not clear experimental evidence. However, it is necessary to remember that in these cases the azeotropic composition occurs at low mole fraction where both experimental methods and models give larger deviations.

Conclusions

New experimental data were measured for different binary systems of ethanol and hydrocarbons with four and five carbon atoms. The experimental results and the parameters of the model used to correlate the data will assist in the optimization of ETBE production plants.

Literature Cited

- DIPPR. *Data Compilation of Pure Compound Properties*; Electronic version DCAPII 4.0; February, 1989.
- Fransson, E.; Barreau, A.; Vidal, J. Vapor–Liquid Equilibrium in Binary Systems of *n*-Pentane + Chlorodifluoromethane or + 1,1-Difluoroethane. *J. Chem. Eng. Data* **1992**, *37*, 521–525.
- Huron, M. J.; Vidal, J. New Mixing Rules in Simple Equations of State for Representing Vapor–Liquid Equilibria of Strongly Nonideal Mixtures. *Fluid Phase Equilib.* **1979**, *3*, 255–271.
- Péneloux, A.; Rauzy, E. A Consistent Correction for Redlich–Kwong–Soave Volumes. *Fluid Phase Equilib.* **1982**, *8*, 7–23.
- Peng, D. Y.; Robinson, D. B. A New Two Constant Equation of State. *Ind. Eng. Chem. Fundam.* **1976**, *15*, 59–64.
- Renon, H.; Prausnitz, J. M. Local Composition in Thermodynamic Excess Functions for Liquid Mixtures. *AIChE J.* **1968**, *14*, 135–144.
- Soave, G. Equilibrium Constants from a Modified Redlich–Kwong Equation of State. *Chem Eng. Sci.* **1972**, *27*, 1197–1203.

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